

# Fast Parsing for Probabilistic Head-driven Phrase Structure Grammars

## Abstract

We present a fast parsing algorithm for probabilistic Head-driven Phrase Structure Grammars (HPSG). The parser can integrate semantic and syntactic preference into figures-of-merit (FOMs) with the *equivalence class function* during parsing, and reduce the search space by dynamic programming on the integrated FOMs. We apply a beam thresholding technique to the parsing algorithm and evaluated its effectiveness on the Penn Treebank corpus. Experimental results show that the parser achieves about 30 times speedup with slight (3 - 4%) loss of recall compared to the conventional parser with CFG filtering.

## 1 Introduction

Probabilistic modeling of unification-based grammars including HPSG (Pollard and Sag, 1994) has received a great deal of attention for the last decade. Log-linear (or Maximum Entropy) modeling provides promising framework for HPSG in terms of estimating model parameters (Abney, 1997; Johnson et al., 1999; Miyao et al., 2003).

The computational cost required for parsing is another major concern for probabilistic HPSG. A naive way to obtain the Viterbi (highest probability) parse given a probabilistic model is to first perform parsing without using probabilities, and then select the highest probability parse by looking at

every parse result. However, such an exhaustive search is often impractical or impossible.

This paper presents a framework for efficient HPSG parsing to obtain the Viterbi parse given a probabilistic model. We define the *equivalence class function* to reduce multiple feature structures to a single feature structure that gives the same resulting figure-of-merit (FOM). With this function, the parser can integrate semantic and syntactic preference into FOMs during parsing, and reduce the search space by dynamic programming on the integrated FOMs.

We present the CKY parsing algorithm using the equivalence class function for probabilistic HPSG. In order to build a fast parser, we apply a beam thresholding technique to the parsing algorithm. The performance of the parser is evaluated on the Penn Treebank corpus.

This paper is organized as follows. Section 2 describes the previous work for efficient parsing with the grammars like HPSG. Section 3 gives the definitions of the probabilistic HPSG. Section 4 presents the equivalence class function and the CKY parsing algorithm using this function. Experimental results using the Penn Treebank corpus are presented in Section 5. Section 6 offers some concluding remarks.

## 2 Related work

Many of the methods for improving parsing efficiency of deep linguistic analysis have been studied in the frameworks of grammars such as Lexical Functional Grammar (LFG) (Bresnan, 1982), Lexicalized Tree Adjoining Grammar (LTAG)

(Shabes et al., 1988), Head-driven Phrase Structure Grammars (Pollard and Sag, 1994), and Combinatory Categorical Grammar (CCG) (Steedman, 2000). Most of them are proposed for full parsing, i.e., all-paths search without FOM (Matsumoto et al., 1983; Maxwell and Kaplan, 1993; van Noord, 1997; Kiefer et al., 1999; Malouf et al., 2000; Torisawa et al., 2000; Penn and Munteanu, 2003). The full parsing strategy is widely used in grammar development, training of parameters for the probabilistic models, or finding the most probable parse among all parses derived by full parsing. However, full parsing is far too expensive in practice because it exhaustively searches all parses derived by the given grammar, especially in case of automatically acquired wide-coverage grammars.

Deep linguistic analysis by unification-based grammars is employed in the VERBMOBIL spontaneous speech translation system (Wahlster, 1993; Kasper et al., 1996). Because their system supposes real-time processing of spontaneous speech, efficiency and robustness were their great concern. Kasper et al. (1996) proposed a probabilistic model where probabilities are assigned to the CFG backbone of the unification-based grammar, and the most probable parse is found by PCFG parsing. After PCFG parsing, the most probable CFG parse is selected and re-parsed by the original unification-based grammar. This process is repeated until parsing by the original unification-based grammar succeeds. Their probabilistic model is based on PCFG and not the probabilistic unification-based grammar parsing.

Geman and Johnson (2002) proposed a dynamic programming algorithm for finding the most probable parse in a packed parse forest generated by unification-based grammars. Their strategy is to first perform full parsing without using probabilities, and then select the highest probability parse without expanding packed parse forest. The behavior of their algorithm is like the Viterbi algorithm for PCFG, and hence the correct parse of the highest probability is guaranteed. The interesting idea of their approach is to first enforce full parsing because the probabilities of non-local dependencies, which cannot be computed during parsing, can be computed after full parsing. However, their efficiency is inherently limited by the

inefficiency of full parsing and the Viterbi algorithm.

Many algorithms for improving efficiency of PCFG parsing are extensively studied including grammar compilation (Tomita, 1986; Nederhof, 2000), the Viterbi algorithm, controlling search strategies without FOM such as left-corner parsing (Rosenkrantz and Lewis II, 1970) or head-corner parsing (Kay, 1970; van Noord, 1997), and with FOM such as the beam search, the best-first search or A\* search (Chitrao and Grishman, 1990; Caraballo and Charniak, 1998; Collins, 1999; Ratnaparkhi, 1999; Roark, 2001; Klein and Manning, 2003). The beam search or the best-first search significantly reduces the time required for finding the best parse at the cost of losing guarantee of correct parse. However, their algorithms cannot simply be applied to the probabilistic unification-based grammar parsing because they assume the locality of probabilities, which cannot be assumed in probabilistic models of unification-based grammars. For example, non-local constraints in unification-based grammars, such as constraints for wh-movement or predicate argument relations, break the locality of probabilities. This is mainly because the PCFG parsing has a coincidence of the locality of the probability and the locality of the process, which the probabilistic unification-based grammar parsing does not have.

### 3 Probabilistic model of HPSG

In HPSG, a small number of schemata explain general grammatical constraints, while a large number of lexical entries express word-specific characteristics. Both schemata and lexical entries are represented by typed feature structures, and constraints represented by feature structures are checked with *unification* (for details, see (Pollard and Sag, 1994)). Figure 1 shows an example of HPSG parsing of the sentence “*Spring has come.*” First, each of the lexical entries for “*has*” and “*come*” is unified with a daughter feature structure of the Head-Complement Schema. Unification provides the phrasal sign of the mother. The sign of the larger constituent is obtained by repeatedly applying schemata to lexical/phrasal signs. Finally, the parse result is output as a phrasal sign that dominates the entire sentence.

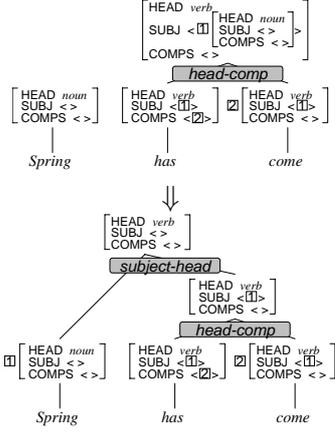


Figure 1: HPSG parsing

Given set  $\mathcal{W}$  of words and set  $\mathcal{F}$  of feature structures, an HPSG grammar is formulated as follows.

**Definition 1 (HPSG grammar)** An HPSG grammar is a tuple,  $G = \langle L, R \rangle$ , where

- $L = \{l = \langle w, F \rangle | w \in \mathcal{W}, F \in \mathcal{F}\}$  is a set of lexical entries, and
- $R$  is a set of grammar rules, i.e.,  $r \in R$  is a partial function:  $\mathcal{F} \times \mathcal{F} \rightarrow \mathcal{F}$ .

Given a sentence, an HPSG grammar computes a set of phrasal signs, i.e., feature structures, as a result of parsing.

Existing studies (Abney, 1997; Johnson et al., 1999; Miyao et al., 2003) define a probability of feature structure  $F$  with *log-linear model* or *maximum entropy model* as follows.

**Definition 2 (Probabilistic HPSG)** Probability  $p(F|\mathbf{w})$  of feature structure  $F$  assigned to given sentence  $\mathbf{w}$  is defined as follows.

$$p(F|\mathbf{w}) = \frac{1}{Z_{\mathbf{w}}} \exp \left( \sum_i \lambda_i \sigma(s_i, F) \right)$$

$$Z_{\mathbf{w}} = \sum_{F'} \exp \left( \sum_i \lambda_i \sigma(s_i, F') \right)$$

where  $\lambda_i$  is a model parameter,  $s_i$  is a fragment of a feature structure, and  $\sigma(s_i, F)$  is a function to return the number of appearances of feature structure fragment  $s_i$  in  $F$ .

Intuitively, a probability is defined as a normalized product of the weights  $\exp(\lambda_i)$  when fragment  $s_i$  appears in the feature structure  $F$ . The probability represents syntactic/semantic preference expressed in a feature structure. For example, in the probabilistic model of predicate-argument structures (Miyao et al., 2003),  $s_i$  was designed to be each predicate-argument relation.

## 4 CKY parsing for probabilistic HPSG

The CKY algorithm, which is essentially a bottom-up parser, is a natural choice for non-probabilistic HPSG parsers. Because the large portion of constraints is expressed in lexical entries in HPSG, bottom-up parsers can utilize those constraints to reduce the search space in early stages of parsing.

For PCFG, extending the CKY algorithm to output the Viterbi parse is straightforward (Ney, 1991; Jurafsky and Martin, 2000). The parser can efficiently calculate the Viterbi parse by taking the maximum of the probabilities of the same nonterminal symbol in each cell.

To achieve such efficiency in CKY parsing for probabilistic HPSG, we need a function to reduce multiple feature structures that are equivalent in terms of resulting FOMs to a single feature structure.

### 4.1 Equivalence class function

First, we define the FOM of feature structure  $F$  as

$$\Delta(F) = \sum_i \lambda_i \sigma(s_i, F),$$

and  $\delta(r, F_1, F_2)$  as

$$\delta(r, F_1, F_2) = \Delta(F) - \Delta(F_1) - \Delta(F_2),$$

$$F = r(F_1, F_2),$$

where  $r$  is a grammar rule, and  $F_1$  and  $F_2$  are the daughters of  $F$ .

We define *equivalence class function*  $\eta$  as a function  $\eta : \mathcal{F} \rightarrow \mathcal{F}$  that satisfies the following conditions for all  $F_1, F_2$  and  $r$ .

**Condition 1:**

$$\exists F. (F = \eta(r(F_1, F_2)) \Leftrightarrow F = \eta(r(\eta(F_1), \eta(F_2))))$$

## Condition 2:

$$\exists d.(d = \delta(r, F_1, F_2) \Leftrightarrow d = \delta(r, \eta(F_1), \eta(F_2)))$$

The first condition guarantees that the parsing with reduced feature structures will not overgenerate nor undergenerate. The second assures that the FOM computed with reduced feature structures is equivalent to the original one.

If we can construct the equivalence class function for a given grammar, we can calculate the FOM of the mother as

$$\Delta(F) = \delta(r, \eta(F_1), \eta(F_2)) + \Delta(F_1) + \Delta(F_2).$$

This equation indicates that we can employ dynamic programming on reduced feature structures in CKY parsing. The remaining issue is how to construct the equivalence class function, which depends on the grammar and the FOM model.

Miyao et al. (2003) implicitly defined an equivalence class function for predicate argument structures. In their definition, instantiated arguments were removed from predicate argument structures in each step of parsing, because instantiated arguments were no more required for further processing in their probabilistic model. Owing to this function, predicate argument structures could be represented with a compact packed structure, which allowed the tractable estimation of model parameters. We formulate their approach as an equivalence class function and state necessary conditions for the function.

## 4.2 CKY parsing algorithm

Figure 2 shows a CKY parsing algorithm for Probabilistic HPSG. The algorithm is almost identical to the CKY for PCFG. Note that a feature structure is reduced by the equivalence class function just before whose FOM is compared with that of the corresponding feature structure which is already in the chart.

## 4.3 Beam thresholding

The CKY algorithm with the equivalent class function enables us to employ various pruning techniques for efficient parsing.

Beam thresholding is a simple and effective technique to prune edges during parsing. In each

```
function CKY(words, grammar)
{
  # diagonal
  for i = 1 to num_words
    foreach  $F_u \in \{F \mid \langle w_i, F \rangle \in L\}$ 
       $\alpha = \log(P(F_u \rightarrow w_i))$ 
       $F'_u = \eta(F_u)$ 
      if ( $\alpha > \pi[i, i][F'_u]$ ) then
         $\pi[i, i][F'_u] = \alpha$ 

  # the rest of the matrix
  for j = 2 to num_words
    for i = 1 to num_words-j+1
      for k = 1 to j-1
        foreach  $F_s \in \pi[i, k]$ 
          foreach  $F_t \in \pi[i+k, j-k]$ 
            if  $F = r(F_s, F_t)$  has succeeded
               $\alpha = \Delta(F_s) + \Delta(F_t) + \delta(r, F_s, F_t)$ 
               $F' = \eta(F)$ 
              if ( $\alpha > \pi[i, j][F']$ ) then
                 $\pi[i, j][F'] = \alpha$ 
}
```

Figure 2: Pseudocode of CKY parsing for probabilistic HPSG.

cell of the chart, the method keeps only a portion of the edges which have higher FOMs compared to the other edges in the same cell.

In this work, we tried two selection schemes for deciding the edges to be kept in each cell.

- Thresholding by number of edges

Each cell keeps the top  $n$  edges according to their FOMs.

- Thresholding by beam width

Each cell keeps the edges whose FOM is greater than  $\alpha_{max} - w$ , where  $\alpha_{max}$  is the highest FOM among the edges in the cell.

## 5 Experiments

### 5.1 Grammar and probabilistic models

An HPSG grammar used in the experiments was extracted from the Penn Treebank (Marcus et al., 1994) by the method of Miyao et al. (Miyao et al., 2004). The grammar acquired from the Penn Treebank Sections 02–21 (39,598 sentences) consisted of 826 lexical entry templates for 10,809 words. In average, 2.62 lexical entries were assigned to a word.

In order to investigate the effect of beam-thresholding with a different kind of probabilistic

$\gamma$	phrasal category
$pos$	part-of-speech of the head word
$lc$	lexical entry of the head word
$r$	schema
$\delta$	distance between the head words of daughters
$pc$	existence of punctuation between daughters
$\rho$	argument position in a predicate-argument structure

Table 1: Notations in the description of features

	# Features	Data size	Estimation time
<i>syntax</i>	54,345	8.66 GB	76 min
<i>full</i>	56,440	13.15 GB	110 min

Table 2: Space/computational costs of model estimation

models, we prepared two probabilistic models. One was a model using only syntactic features (the *syntax* model). Syntactic features capture the characteristics of each branching in an HPSG derivation. Formally, a syntactic feature represents the occurrence of the branching  $\langle\langle\gamma_h, pos_h, lc_h\rangle, \langle\gamma_n, pos_n, lc_n\rangle, r, \delta, pc\rangle$ , where  $\gamma_h$  and  $\gamma_n$  are for head/non-head daughters and other notations are represented in Table 1. The other was a model using semantic features in addition to the syntactic features (the *full* model). Semantic features capture the characteristics of each predicate-argument relation, which is formally represented with  $\langle\langle pos_h, lc_h\rangle, \langle pos_n, lc_n\rangle, \rho, \delta\rangle$ . Note that the syntax model concerns tree structures of HPSG derivations, while the full model treats predicate-argument structures that can include re-entrant structures. Comparing the behaviors of these models, we can investigate the effect of the equivalent class function in the model involving re-entrant structures. We implemented the equivalence class function similar to the existing study on the probabilistic modeling of predicate-argument structures (Miyao et al., 2003)

Table 2 shows the space/computational costs of model estimation. The parameters of the two models were estimated by using the limited-memory BFGS algorithm (Nocedal, 1980) with a Gaussian distribution as a prior probability distribution for smoothing (Chen and Rosenfeld, 1999). All of the experiments were performed on servers with 1.26-GHz Pentium-III CPU and 4-GB memory.

The sentences in section 22 were used for eval-

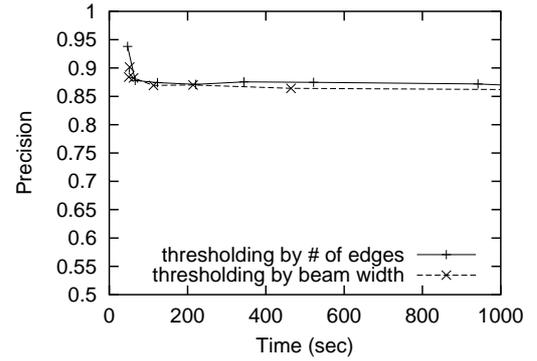


Figure 3: Precision versus time in the syntax model

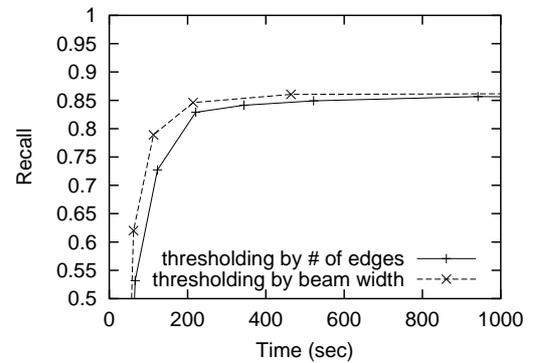


Figure 4: Recall versus time in the syntax model

uation. We parsed 200 sentences that had less than 40 words and could be strictly covered by the grammar (i.e., the grammar included all lexical entries to output the correct parse for the sentence).

## 5.2 Beam thresholding schemes

We first performed experiments to evaluate the beam thresholding schemes presented in section 4.3. We evaluated the accuracy of predicate-argument relations and the total time required for parsing the sentences. Each output was counted as correct if the type of predicate, the argument position, the head word, and the argument word were all correct.

Figure 3 to 4 show the experimental results in the syntax model. It should be noted that beam thresholding does not degrade the precision of the output. As for the recall, thresholding by beam width gives better performance than thresholding by the number of edges.

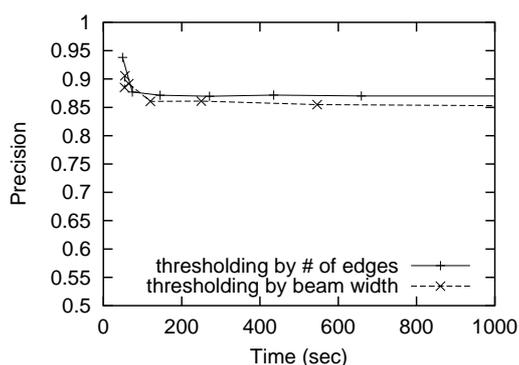


Figure 5: Precision versus time in the full model

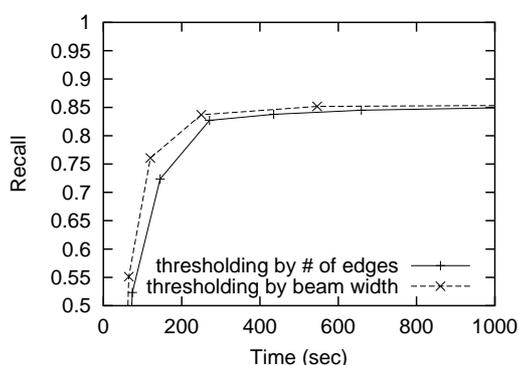


Figure 6: Recall versus time in the full model

The results in the full model are shown in Figure 5 to 6. They show similar trends to those in the syntax model. Thresholding by beam width again gives better performance.

### 5.3 Comparing with the baseline parser

One simple way to obtain the best parse of a sentence is to first parse the sentence without using the probabilistic model, then search the best parse among the parse results. We have implemented this baseline parser with the CKY parsing algorithm for non-probabilistic HPSG combined with a CFG filtering technique (Torisawa et al., 2000).

We compared our parsing method proposed in this paper with the baseline parser with regard to the speed and accuracy of parsing. Table 3 and 4 show the results. The parameter setting of each beam thresholding scheme was chosen so that the time of parsing is around 10% of the baseline parser. We also performed parsing by combining the two thresholding schemes. The parser with the

combined thresholding achieved about 30 times speedup compared with the baseline parser in both probabilistic models. In this parameter setting, the loss of recall was quite small (3 - 4%).

## 6 Conclusion

This paper presented a framework for efficient parsing with probabilistic HPSG with the equivalence class function. The proposed framework enables dynamic programming for probability computation without enforcing full parsing, i.e., the probabilities can be computed during parsing. With this function, the search space can be significantly reduced by various pruning techniques including beam search and best-first search strategies.

We have built a parser using this framework and a beam thresholding technique. Experimental results on the Penn Treebank corpus show that the parser achieves around 30 times speedup with slight loss of recall compared to the conventional parser with CFG filtering.

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Parser	Precision	Recall	Total Time (sec)	Time per Sentence (sec)
Baseline	87.5%	87.7%	4942	24.71
Beam thresholding (n = 12)	87.5%	84.9%	522	2.61
Beam thresholding (w = 6.0)	86.4%	86.1%	464	2.32
Combined (n = 12, w = 6.0)	87.4%	84.6%	184	0.92

Table 3: Comparing with the baseline parser in the syntax model

Parser	Precision	Recall	Total Time (sec)	Time per Sentence (sec)
Baseline	86.9%	87.2%	5328	26.64
Beam thresholding (n = 10)	87.2%	83.8%	435	2.18
Beam thresholding (w = 6.0)	85.5%	85.2%	546	2.73
Combined (n = 10, w = 6.0)	87.5%	83.4%	169	0.85

Table 4: Comparing with the baseline parser in the full model

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